

Math 222, Fall 2007
Matlab Project #2: Direction Fields and Nonlinear ODEs
Due date: November 30, 2007

Adapt the matlab script you developed in Project #1 to use Euler's method with step size $h = 0.01$ to integrate the following IVP:

$$y' = y^2 - t^2, \quad y(0) = y_0,$$

where your script allows you to specify the initial condition y_0 . Using your script, do the following:

1. Do a number of runs to $t = 10$, gradually increasing the initial condition from $y_0 = 0$ to $y_0 = 1$. Note that at a certain value of y_0 , the solution behavior changes significantly. Estimate this critical value of y_0 to at least two significant figures.
2. Plot the direction field using the matlab script `dfield`. To download this script, go to <http://math.rice.edu/~dfield/matlab7/dfield7.m>, then save the file to a local directory using the "Save Page As..." option from the right-click mouse menu. From the matlab command line, make sure the file `dfield7.m` is in your current working directory, then type `dfield7` to run.
3. Use the direction field to explain your result in Part 1.

Format. Your project must be typed on a computer, with the exception of equations, which may be written into blank spaces left in the typed text. All graphs must have a title and axis labels (type `doc plot` at the matlab command line for instructions). Remember to explain your results and to provide sufficient graphical evidence to support them. Include a printout of the script in your project.